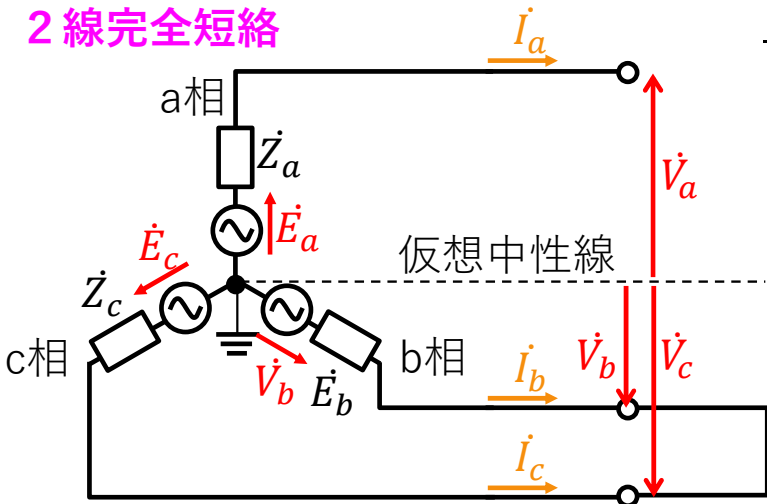


対称座標法 (3) 《無負荷発電機の短絡計算1》

2線完全短絡



回路条件

$$\dot{V}_b = \dot{V}_c \dots \textcircled{1} \quad I_a = 0 \dots \textcircled{2} \quad I_b + I_c = 0 \dots \textcircled{3}$$

$$\textcircled{3} \text{に} \textcircled{4}, \textcircled{5} \text{を代入} \quad 2I_0 = I_1 + I_2$$

$$\textcircled{2}, \textcircled{6} \text{より} I_a = I_0 + I_1 + I_2 = 3I_0 = 0$$

$$\therefore I_0 = 0, I_1 = -I_2 \dots \textcircled{7}$$

$$\textcircled{1} \text{に} \textcircled{8}, \textcircled{9} \text{を代入} \quad \dot{V}_1 = \dot{V}_2 \dots \textcircled{10}$$

$$\textcircled{10} \text{に} \textcircled{7}, \textcircled{11}, \textcircled{12} \text{を代入} \quad I_1 = \frac{E_a}{Z_1 + Z_2} = -I_2 \dots \textcircled{13}$$

④に⑦,⑬を代入

$$I_b = I_0 + a^2 I_1 + a I_2 = \frac{a^2 - a}{Z_1 + Z_2} E_a \dots \textcircled{14}$$

$$\textcircled{3} \text{に} \textcircled{14} \text{を代入} \quad I_c = -I_b = \frac{a - a^2}{Z_1 + Z_2} E_a$$

$$\textcircled{15} \text{に} \textcircled{7} \text{を代入} \quad \dot{V}_0 = -Z_0 I_0 = 0 \dots \textcircled{16}$$

$$\textcircled{11} \text{に} \textcircled{13} \text{を代入} \quad \dot{V}_1 = \frac{Z_2}{Z_1 + Z_2} E_a = \dot{V}_2 \dots \textcircled{17}$$

$$\textcircled{18} \text{に} \textcircled{16}, \textcircled{17} \text{を代入} \quad \dot{V}_a = \frac{2Z_2}{Z_1 + Z_2} E_a$$

$$\textcircled{8} \text{に} \textcircled{16}, \textcircled{17} \text{を代入} \quad \dot{V}_b = -\frac{Z_2}{Z_1 + Z_2} E_a = \dot{V}_c$$

発電機の基本式

$$\begin{cases} \dot{V}_0 = -Z_0 I_0 & \dots \textcircled{15} \\ \dot{V}_1 = E_a - Z_1 I_1 & \dots \textcircled{11} \\ \dot{V}_2 = -Z_2 I_2 & \dots \textcircled{12} \end{cases}$$

電流/電圧の定義式・対称分式

$$\begin{cases} \dot{V}_a = \dot{V}_0 + \dot{V}_1 + \dot{V}_2 & \dots \textcircled{18} \\ \dot{V}_b = \dot{V}_0 + a^2 \dot{V}_1 + a \dot{V}_2 & \dots \textcircled{8} \\ \dot{V}_c = \dot{V}_0 + a \dot{V}_1 + a^2 \dot{V}_2 & \dots \textcircled{9} \\ \dot{V}_0 = \frac{1}{3} (\dot{V}_a + \dot{V}_b + \dot{V}_c) \\ \dot{V}_1 = \frac{1}{3} (\dot{V}_a + a \dot{V}_b + a^2 \dot{V}_c) \\ \dot{V}_2 = \frac{1}{3} (\dot{V}_a + a^2 \dot{V}_b + a \dot{V}_c) \\ I_a = I_0 + I_1 + I_2 & \dots \textcircled{6} \\ I_b = I_0 + a^2 I_1 + a I_2 & \dots \textcircled{4} \\ I_c = I_0 + a I_1 + a^2 I_2 & \dots \textcircled{5} \\ I_0 = \frac{1}{3} (I_a + I_b + I_c) \\ I_1 = \frac{1}{3} (I_a + a I_b + a^2 I_c) \\ I_2 = \frac{1}{3} (I_a + a^2 I_b + a I_c) \end{cases}$$

対称座標法 (3)

2線完全短絡の計算

$$\dot{V}_b = \dot{V}_c \cdots \textcircled{1} \quad \dot{I}_a = 0 \cdots \textcircled{2} \quad \dot{I}_b + \dot{I}_c = 0 \cdots \textcircled{3}$$

③に④,⑤を代入

$$\begin{aligned} \dot{I}_0 + a^2 \dot{I}_1 + a \dot{I}_2 + (\dot{I}_0 + a \dot{I}_1 + a^2 \dot{I}_2) &= 0 \\ 2\dot{I}_0 + (a^2 + a)(\dot{I}_1 + \dot{I}_2) &= 0 \end{aligned}$$

$$a^2 + a = -1 \text{ より } 2\dot{I}_0 = \dot{I}_1 + \dot{I}_2$$

$$\textcircled{2}, \textcircled{6} \text{ より } \dot{I}_a = \dot{I}_0 + \dot{I}_1 + \dot{I}_2 = 3\dot{I}_0 = 0$$

$$\therefore \dot{I}_0 = 0, \dot{I}_1 = -\dot{I}_2 \cdots \textcircled{7}$$

①より $\dot{V}_b - \dot{V}_c = 0$ に⑧,⑨を代入

$$\begin{aligned} \dot{V}_0 + a^2 \dot{V}_1 + a \dot{V}_2 - (\dot{V}_0 + a \dot{V}_1 + a^2 \dot{V}_2) &= 0 \\ (a^2 - a)(\dot{V}_1 - \dot{V}_2) &= 0 \end{aligned}$$

$$a^2 - a \neq 0 \text{ より } \dot{V}_1 = \dot{V}_2 \cdots \textcircled{10}$$

⑩に⑪,⑫,⑦を代入

$$\dot{E}_a - \dot{Z}_1 \dot{I}_1 = -\dot{Z}_2 \dot{I}_2 = \dot{Z}_2 \dot{I}_1$$

$$\dot{I}_1 = \frac{\dot{E}_a}{\dot{Z}_1 + \dot{Z}_2} = -\dot{I}_2 \cdots \textcircled{13}$$

④に⑦,⑬を代入

$$\dot{I}_b = \dot{I}_0 + a^2 \dot{I}_1 + a \dot{I}_2 = \frac{a^2 - a}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a \cdots \textcircled{14}$$

$$\textcircled{3} \text{ に } \textcircled{14} \text{ を代入 } \dot{I}_c = -\dot{I}_b = \frac{a - a^2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a$$

$$\textcircled{15} \text{ に } \textcircled{7} \text{ を代入 } \dot{V}_0 = -\dot{Z}_0 \dot{I}_0 = 0 \cdots \textcircled{16}$$

⑪に⑬を代入

$$\dot{V}_1 = \dot{E}_a - \frac{\dot{Z}_1 \dot{E}_a}{\dot{Z}_1 + \dot{Z}_2} = \frac{\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a = \dot{V}_2 \cdots \textcircled{17}$$

⑱に⑯,⑰を代入

$$\dot{V}_a = 0 + \frac{\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a + \frac{\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a = \frac{2\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a$$

⑧に⑯,⑰を代入

$$\begin{aligned} \dot{V}_b &= 0 + \frac{a^2 \dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a + \frac{a \dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a = \frac{(a^2 + a) \dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a \\ &= -\frac{\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2} \dot{E}_a = \dot{V}_c \end{aligned}$$

発電機の基本式

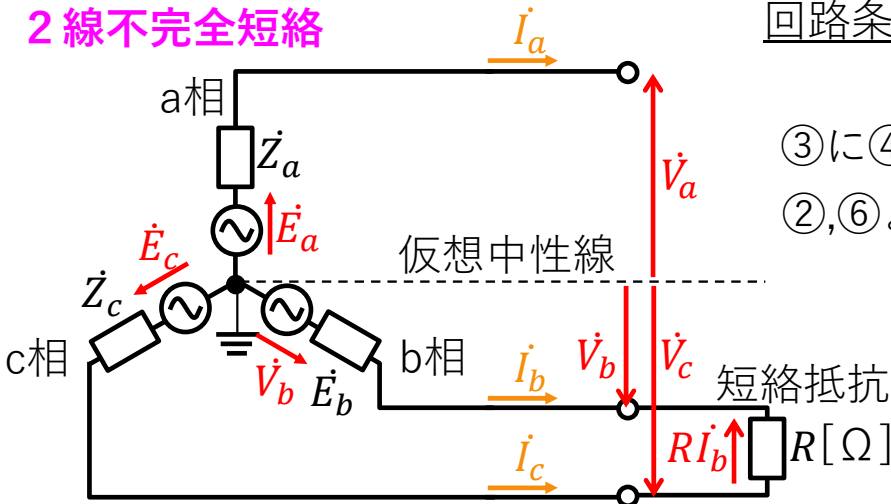
$$\begin{cases} \dot{V}_0 = -\dot{Z}_0 \dot{I}_0 & \cdots \textcircled{15} \\ \dot{V}_1 = \dot{E}_a - \dot{Z}_1 \dot{I}_1 & \cdots \textcircled{11} \\ \dot{V}_2 = -\dot{Z}_2 \dot{I}_2 & \cdots \textcircled{12} \end{cases}$$

電流/電圧の定義式・対称分式

$$\begin{cases} \dot{V}_a = \dot{V}_0 + \dot{V}_1 + \dot{V}_2 & \cdots \textcircled{18} \\ \dot{V}_b = \dot{V}_0 + a^2 \dot{V}_1 + a \dot{V}_2 & \cdots \textcircled{8} \\ \dot{V}_c = \dot{V}_0 + a \dot{V}_1 + a^2 \dot{V}_2 & \cdots \textcircled{9} \\ \dot{V}_0 = \frac{1}{3}(\dot{V}_a + \dot{V}_b + \dot{V}_c) \\ \dot{V}_1 = \frac{1}{3}(\dot{V}_a + a \dot{V}_b + a^2 \dot{V}_c) \\ \dot{V}_2 = \frac{1}{3}(\dot{V}_a + a^2 \dot{V}_b + a \dot{V}_c) \\ \dot{I}_a = \dot{I}_0 + \dot{I}_1 + \dot{I}_2 & \cdots \textcircled{6} \\ \dot{I}_b = \dot{I}_0 + a^2 \dot{I}_1 + a \dot{I}_2 & \cdots \textcircled{4} \\ \dot{I}_c = \dot{I}_0 + a \dot{I}_1 + a^2 \dot{I}_2 & \cdots \textcircled{5} \\ \dot{I}_0 = \frac{1}{3}(\dot{I}_a + \dot{I}_b + \dot{I}_c) \\ \dot{I}_1 = \frac{1}{3}(\dot{I}_a + a \dot{I}_b + a^2 \dot{I}_c) \\ \dot{I}_2 = \frac{1}{3}(\dot{I}_a + a^2 \dot{I}_b + a \dot{I}_c) \end{cases}$$

対称座標法 (3) 《無負荷発電機の短絡計算2》

2線不完全短絡



回路条件 $\dot{V}_b - \dot{V}_c = RI_b \dots \textcircled{1}$

$I_a = 0 \dots \textcircled{2}$ $I_b + I_c = 0 \dots \textcircled{3}$

③に④,⑤を代入 $2I_0 = I_1 + I_2$

②,⑥より $I_a = I_0 + I_1 + I_2 = 3I_0 = 0$

$\therefore I_0 = 0, I_1 = -I_2 \dots \textcircled{7}$

①に④,⑦,⑧,⑨を代入

$\dot{V}_1 - \dot{V}_2 = RI_1 \dots \textcircled{10}$

⑩に⑪,⑫,⑦を代入

$I_1 = \frac{E_a}{Z_1 + Z_2 + R} = -I_2 \dots \textcircled{13}$

④に⑦,⑬を代入

$I_b = \frac{a^2 - a}{Z_1 + Z_2 + R} E_a \dots \textcircled{14}$ $I_c = -I_b = \frac{a - a^2}{Z_1 + Z_2 + R} E_a$

③に⑭を代入

⑮に⑦を代入

$\dot{V}_0 = -Z_0 I_0 = 0 \dots \textcircled{16}$

⑪に⑬を代入

$\dot{V}_1 = \frac{Z_2 + R}{Z_1 + Z_2 + R} E_a \dots \textcircled{17}$

⑫に⑬を代入

$\dot{V}_2 = \frac{Z_2}{Z_1 + Z_2 + R} E_a \dots \textcircled{18}$

⑰に⑱,⑲,⑳を代入

$\dot{V}_a = \frac{2Z_2 + R}{Z_1 + Z_2 + R} E_a$

⑧に⑱,⑲,⑳を代入

$\dot{V}_b = \frac{-Z_2 + a^2 R}{Z_1 + Z_2 + R} E_a$

⑨に⑱,⑲,⑳を代入

$\dot{V}_c = \frac{-Z_2 + aR}{Z_1 + Z_2 + R} E_a$

発電機の基本式

$\dot{V}_0 = -Z_0 I_0 \dots \textcircled{15}$

$\dot{V}_1 = E_a - Z_1 I_1 \dots \textcircled{11}$

$\dot{V}_2 = -Z_2 I_2 \dots \textcircled{12}$

電流/電圧の定義式・対称分式

$\dot{V}_a = \dot{V}_0 + \dot{V}_1 + \dot{V}_2 \dots \textcircled{19}$

$\dot{V}_b = \dot{V}_0 + a^2 \dot{V}_1 + a \dot{V}_2 \dots \textcircled{8}$

$\dot{V}_c = \dot{V}_0 + a \dot{V}_1 + a^2 \dot{V}_2 \dots \textcircled{9}$

$\dot{V}_0 = \frac{1}{3} (\dot{V}_a + \dot{V}_b + \dot{V}_c)$

$\dot{V}_1 = \frac{1}{3} (\dot{V}_a + a \dot{V}_b + a^2 \dot{V}_c)$

$\dot{V}_2 = \frac{1}{3} (\dot{V}_a + a^2 \dot{V}_b + a \dot{V}_c)$

$I_a = I_0 + I_1 + I_2 \dots \textcircled{6}$

$I_b = I_0 + a^2 I_1 + a I_2 \dots \textcircled{4}$

$I_c = I_0 + a I_1 + a^2 I_2 \dots \textcircled{5}$

$I_0 = \frac{1}{3} (I_a + I_b + I_c)$

$I_1 = \frac{1}{3} (I_a + a I_b + a^2 I_c)$

$I_2 = \frac{1}{3} (I_a + a^2 I_b + a I_c)$

対称座標法 (2) 2線不完全短絡の計算

$$\dot{V}_b - \dot{V}_c = R\dot{I}_b \quad \dots \textcircled{1}$$

$$\dot{I}_a = 0 \quad \dots \textcircled{2} \quad \dot{I}_b + \dot{I}_c = 0 \quad \dots \textcircled{3}$$

③に④,⑤を代入

$$\dot{I}_0 + a^2\dot{I}_1 + a\dot{I}_2 + (\dot{I}_0 + a\dot{I}_1 + a^2\dot{I}_2) = 0$$

$$2\dot{I}_0 + (a^2 + a)(\dot{I}_1 + \dot{I}_2) = 0$$

$$a^2 + a = -1 \text{ より } 2\dot{I}_0 = \dot{I}_1 + \dot{I}_2$$

$$\textcircled{2}, \textcircled{6} \text{ より } \dot{I}_a = \dot{I}_0 + \dot{I}_1 + \dot{I}_2 = 3\dot{I}_0 = 0$$

$$\therefore \dot{I}_0 = 0, \dot{I}_1 = -\dot{I}_2 \quad \dots \textcircled{7}$$

①より $\dot{V}_b - \dot{V}_c = R\dot{I}_b$ に④,⑦,⑧,⑨を代入

$$\dot{V}_0 + a^2\dot{V}_1 + a\dot{V}_2 - (\dot{V}_0 + a\dot{V}_1 + a^2\dot{V}_2) = R\dot{I}_b$$

$$(a^2 - a)(\dot{V}_1 - \dot{V}_2) = R(\dot{I}_0 + a^2\dot{I}_1 + a\dot{I}_2)$$

$$(a^2 - a)(\dot{V}_1 - \dot{V}_2) = R(a^2 - a)\dot{I}_1$$

$$\dot{V}_1 - \dot{V}_2 = R\dot{I}_1 \quad \dots \textcircled{10}$$

⑩に⑪,⑫,⑦を代入

$$\dot{E}_a - \dot{Z}_1\dot{I}_1 - \dot{Z}_2\dot{I}_2 = \dot{E}_a - (\dot{Z}_1 + \dot{Z}_2)\dot{I}_1 = R\dot{I}_1$$

$$\dot{I}_1 = \frac{\dot{E}_a}{\dot{Z}_1 + \dot{Z}_2 + R} = -\dot{I}_2 \quad \dots \textcircled{13}$$

④に⑦,⑬を代入

$$\dot{I}_b = \dot{I}_0 + a^2\dot{I}_1 + a\dot{I}_2 = \frac{a^2 - a}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a \quad \dots \textcircled{14}$$

$$\textcircled{3} \text{ に } \textcircled{14} \text{ を代入 } \dot{I}_c = -\dot{I}_b = \frac{a - a^2}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a$$

$$\textcircled{15} \text{ に } \textcircled{7} \text{ を代入 } \dot{V}_0 = -\dot{Z}_0\dot{I}_0 = 0 \quad \dots \textcircled{16}$$

⑪に⑬を代入

$$\dot{V}_1 = \dot{E}_a - \frac{\dot{Z}_1\dot{E}_a}{\dot{Z}_1 + \dot{Z}_2 + R} = \frac{\dot{Z}_2 + R}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a \quad \dots \textcircled{17}$$

$$\textcircled{12} \text{ に } \textcircled{13} \text{ を代入 } \dot{V}_2 = \frac{\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a \quad \dots \textcircled{18}$$

⑱に⑯,⑰,⑱を代入

$$\dot{V}_a = \frac{\dot{Z}_2 + R}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a + \frac{\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a = \frac{2\dot{Z}_2 + R}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a$$

⑧に⑯,⑰,⑱を代入

$$\begin{aligned} \dot{V}_b &= \frac{a^2(\dot{Z}_2 + R)}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a + \frac{a\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a \\ &= \frac{(a^2 + a)\dot{Z}_2 + a^2R}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a = \frac{-\dot{Z}_2 + a^2R}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a \end{aligned}$$

⑨に⑯,⑰,⑱を代入

$$\dot{V}_c = \frac{a(\dot{Z}_2 + R)}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a + \frac{a^2\dot{Z}_2}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a = \frac{-\dot{Z}_2 + aR}{\dot{Z}_1 + \dot{Z}_2 + R} \dot{E}_a$$

発電機の基本式

$$\begin{cases} \dot{V}_0 = -\dot{Z}_0\dot{I}_0 & \dots \textcircled{15} \\ \dot{V}_1 = \dot{E}_a - \dot{Z}_1\dot{I}_1 & \dots \textcircled{11} \\ \dot{V}_2 = -\dot{Z}_2\dot{I}_2 & \dots \textcircled{12} \end{cases}$$

電流/電圧の定義式・対称分式

$$\begin{cases} \dot{V}_a = \dot{V}_0 + \dot{V}_1 + \dot{V}_2 & \dots \textcircled{19} \\ \dot{V}_b = \dot{V}_0 + a^2\dot{V}_1 + a\dot{V}_2 & \dots \textcircled{8} \\ \dot{V}_c = \dot{V}_0 + a\dot{V}_1 + a^2\dot{V}_2 & \dots \textcircled{9} \end{cases}$$

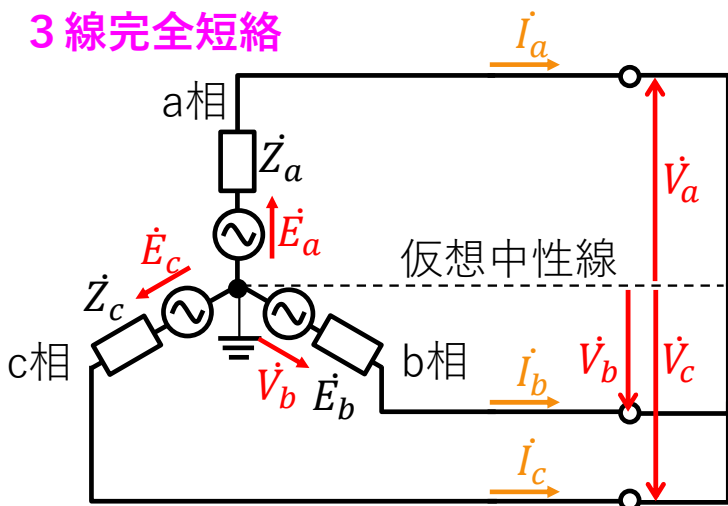
$$\begin{cases} \dot{V}_0 = \frac{1}{3}(\dot{V}_a + \dot{V}_b + \dot{V}_c) \\ \dot{V}_1 = \frac{1}{3}(\dot{V}_a + a\dot{V}_b + a^2\dot{V}_c) \\ \dot{V}_2 = \frac{1}{3}(\dot{V}_a + a^2\dot{V}_b + a\dot{V}_c) \end{cases}$$

$$\begin{cases} \dot{I}_a = \dot{I}_0 + \dot{I}_1 + \dot{I}_2 & \dots \textcircled{6} \\ \dot{I}_b = \dot{I}_0 + a^2\dot{I}_1 + a\dot{I}_2 & \dots \textcircled{4} \\ \dot{I}_c = \dot{I}_0 + a\dot{I}_1 + a^2\dot{I}_2 & \dots \textcircled{5} \end{cases}$$

$$\begin{cases} \dot{I}_0 = \frac{1}{3}(\dot{I}_a + \dot{I}_b + \dot{I}_c) \\ \dot{I}_1 = \frac{1}{3}(\dot{I}_a + a\dot{I}_b + a^2\dot{I}_c) \\ \dot{I}_2 = \frac{1}{3}(\dot{I}_a + a^2\dot{I}_b + a\dot{I}_c) \end{cases}$$

対称座標法 (3) 《無負荷発電機の短絡計算3》

3線完全短絡



回路条件 $I_a + I_b + I_c = 0 \dots \textcircled{1}$

$V_a = V_b = V_c \dots \textcircled{2}$

①,③より $I_0 = \frac{1}{3}(I_a + I_b + I_c) = 0 \dots \textcircled{4}$

④,⑤より $V_0 = -Z_0 I_0 = 0 \dots \textcircled{6}$

②,⑦より $V_1 = \frac{1}{3}(1 + a + a^2)V_a = 0 \dots \textcircled{9}$

②,⑧より $V_2 = \frac{1}{3}(1 + a^2 + a)V_a = 0 \dots \textcircled{10}$

⑥,⑨,⑩より $V_0 = V_1 = V_2 = 0 \dots \textcircled{11}$

⑪,⑫,⑬,⑭より $V_a = V_b = V_c = 0$

3線完全地絡と同じ回路条件

$\therefore I_a = \frac{E_a}{Z_1} \quad I_b = \frac{a^2 E_a}{Z_1} \quad I_c = \frac{a E_a}{Z_1}$

$Z_1 = Z_2 = Z$ のとき、3線完全短絡電流 I_{s3} と 2線完全短絡電流 I_{s2} の大きさは

$|I_{s3}| = \left| \frac{E_a}{Z} \right| = \frac{E}{Z} \quad |I_{s2}| = \left| \frac{a^2 - a}{Z + Z} E_a \right| = \left| \frac{j\sqrt{3}}{2Z} E_a \right| = \frac{\sqrt{3}}{2} \cdot \frac{E}{Z} \quad |I_{s2}| = \frac{\sqrt{3}}{2} |I_{s3}| \doteq 0.87 |I_{s3}|$

発電機の基本式

$\begin{cases} V_0 = -Z_0 I_0 \dots \textcircled{5} \\ V_1 = E_a - Z_1 I_1 \\ V_2 = -Z_2 I_2 \end{cases}$

電流/電圧の定義式・対称分式

$\begin{cases} V_a = V_0 + V_1 + V_2 \dots \textcircled{12} \\ V_b = V_0 + a^2 V_1 + a V_2 \dots \textcircled{13} \\ V_c = V_0 + a V_1 + a^2 V_2 \dots \textcircled{14} \\ V_0 = \frac{1}{3}(V_a + V_b + V_c) \\ V_1 = \frac{1}{3}(V_a + a V_b + a^2 V_c) \dots \textcircled{7} \\ V_2 = \frac{1}{3}(V_a + a^2 V_b + a V_c) \dots \textcircled{8} \end{cases}$

$\begin{cases} I_a = I_0 + I_1 + I_2 \\ I_b = I_0 + a^2 I_1 + a I_2 \\ I_c = I_0 + a I_1 + a^2 I_2 \\ I_0 = \frac{1}{3}(I_a + I_b + I_c) \dots \textcircled{3} \\ I_1 = \frac{1}{3}(I_a + a I_b + a^2 I_c) \\ I_2 = \frac{1}{3}(I_a + a^2 I_b + a I_c) \end{cases}$